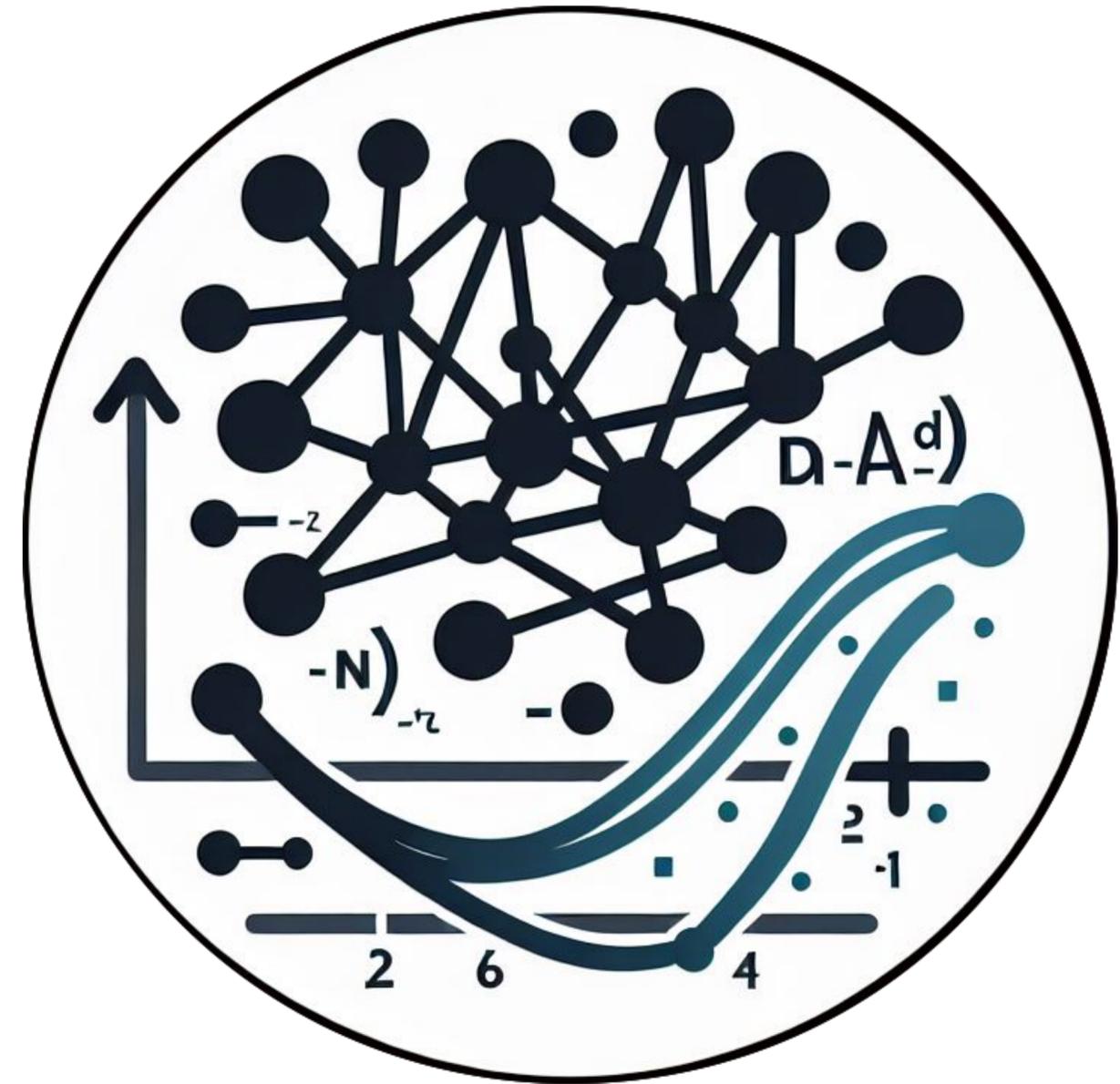


# Convolutional Neural Nets



Deep Learning for Engineers

Andrew Ning

[aning@byu.edu](mailto:aning@byu.edu)

# What do we use Neural ODEs for?

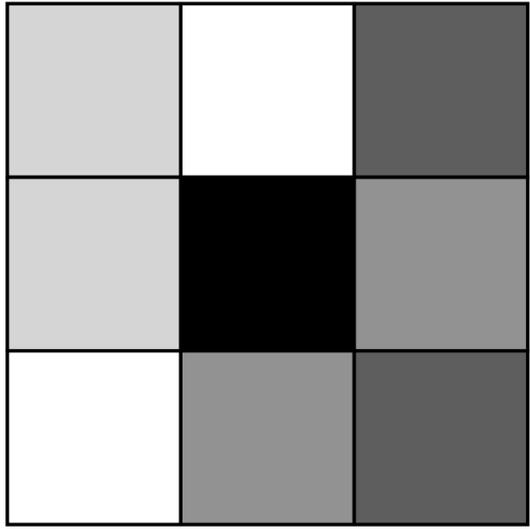
Predict forward in time (e.g., weather problem)

Predict different initial conditions/parameters

Increase or reduce dimensionality to make problem better behaved numerically, or linear, etc.

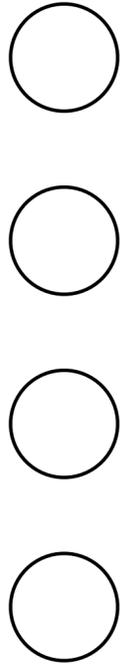
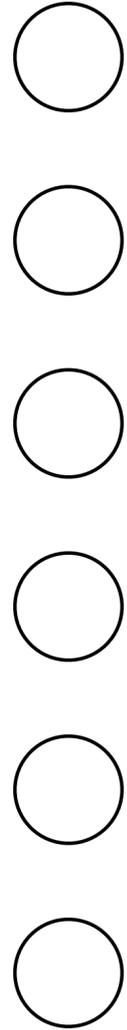
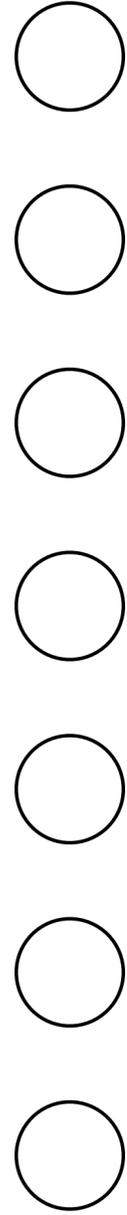
Symbolic regression

Speed



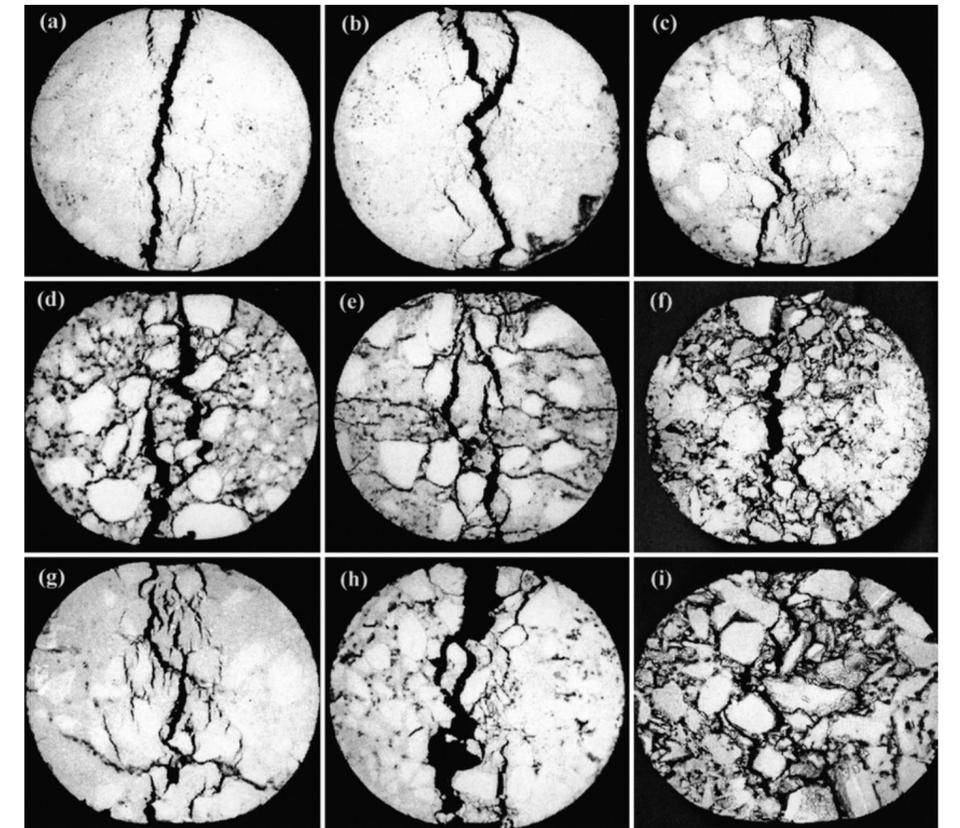
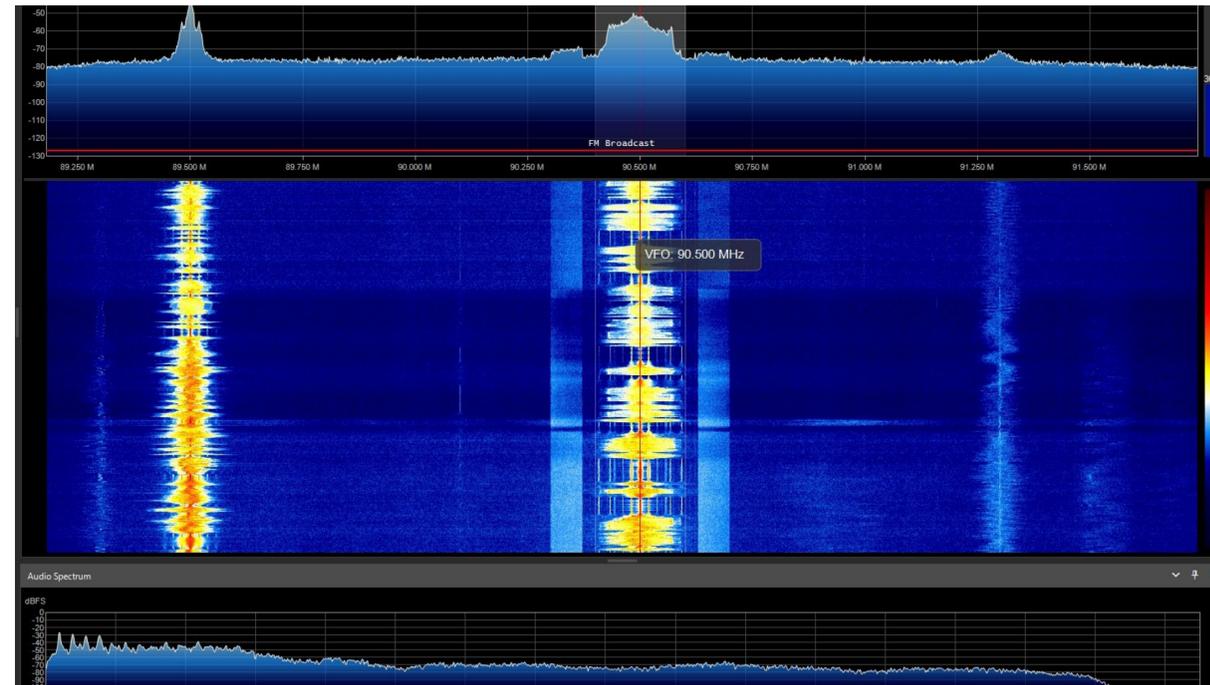
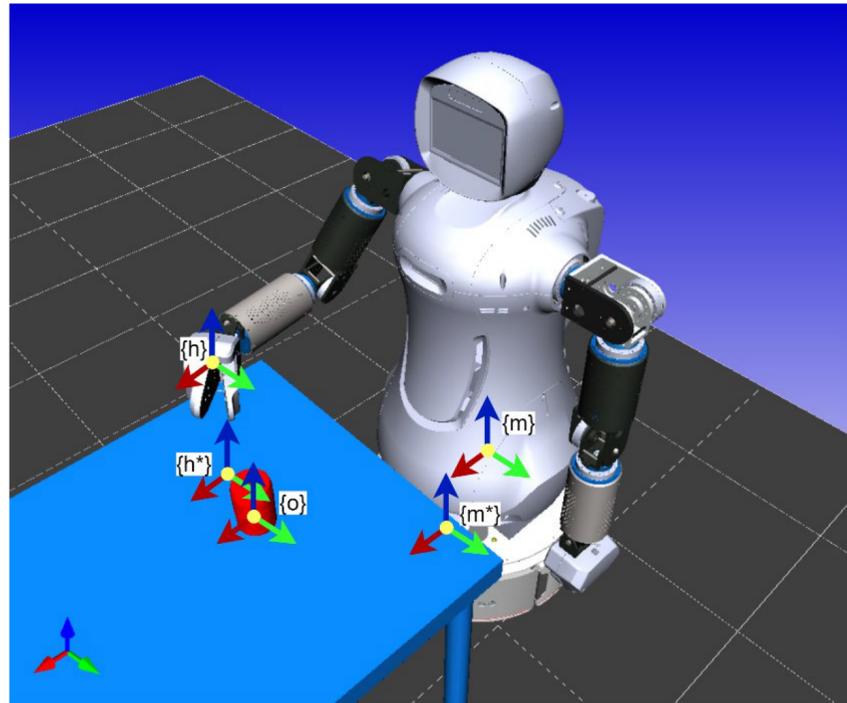
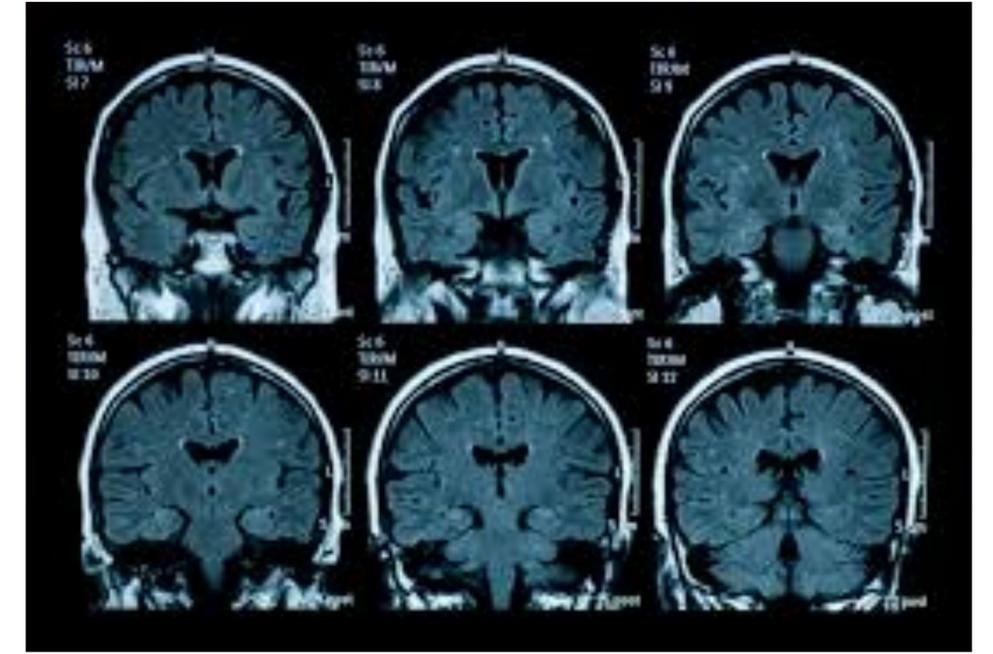
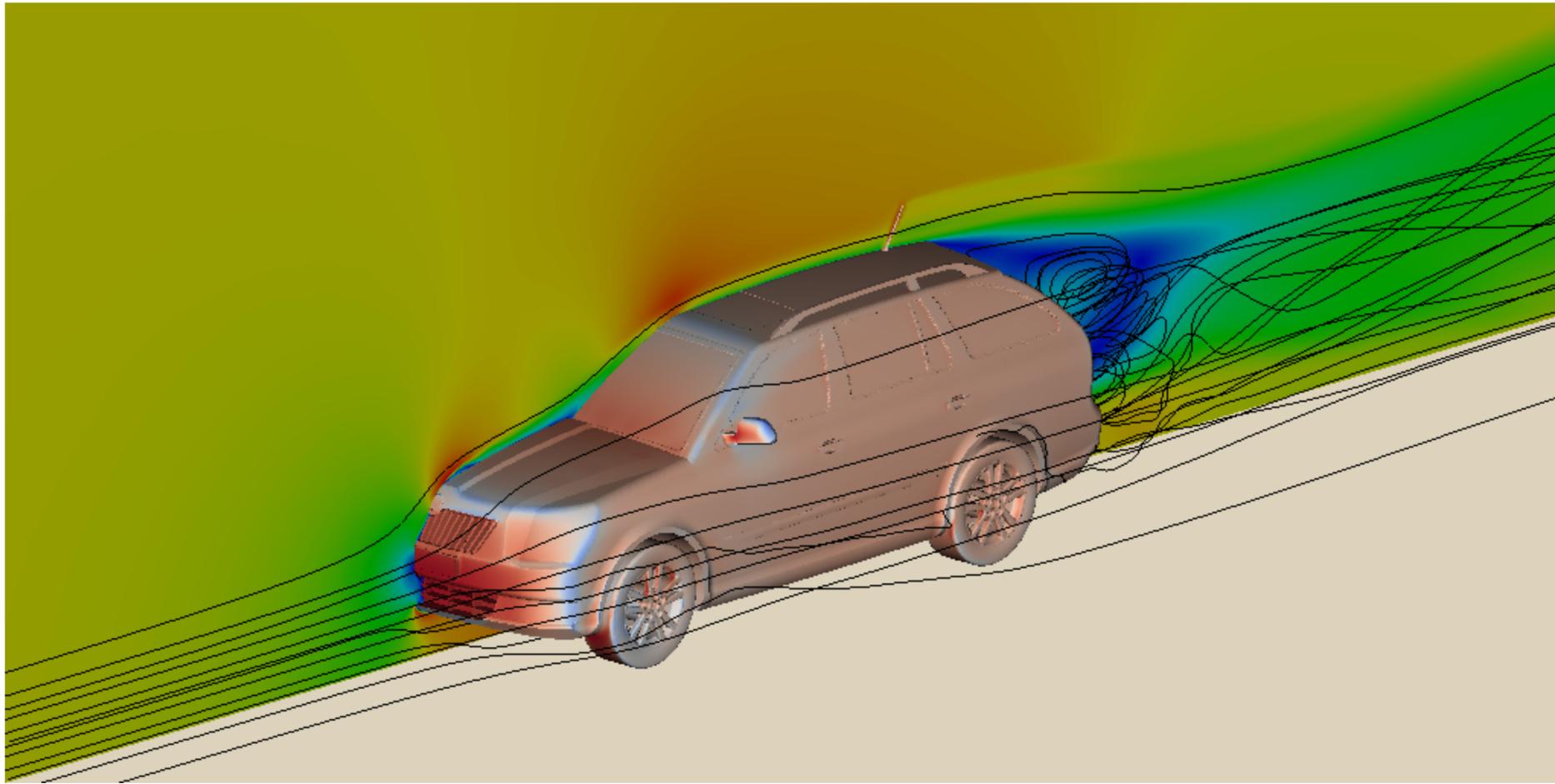
|     |    |     |
|-----|----|-----|
| .75 | 1  | .25 |
| .75 | 0  | .5  |
| 1   | .5 | .25 |

|     |
|-----|
| .75 |
| 1   |
| .25 |
| .75 |
| 0   |
| .5  |
| 1   |
| .5  |
| .25 |





<https://www.cs.montana.edu/courses/fall2006/430/lectures/02/lect02.html>



# Kernel

|   |   |   |
|---|---|---|
| 0 | 1 | 2 |
| 2 | 2 | 0 |
| 0 | 1 | 2 |

|                |                |                |   |   |
|----------------|----------------|----------------|---|---|
| 3 <sub>0</sub> | 3 <sub>1</sub> | 2 <sub>2</sub> | 1 | 0 |
| 0 <sub>2</sub> | 0 <sub>2</sub> | 1 <sub>0</sub> | 3 | 1 |
| 3 <sub>0</sub> | 1 <sub>1</sub> | 2 <sub>2</sub> | 2 | 3 |
| 2              | 0              | 0              | 2 | 2 |
| 2              | 0              | 0              | 0 | 1 |

|      |      |      |
|------|------|------|
| 12.0 | 12.0 | 17.0 |
| 10.0 | 17.0 | 19.0 |
| 9.0  | 6.0  | 14.0 |

|   |                |                |                |   |
|---|----------------|----------------|----------------|---|
| 3 | 3 <sub>0</sub> | 2 <sub>1</sub> | 1 <sub>2</sub> | 0 |
| 0 | 0 <sub>2</sub> | 1 <sub>2</sub> | 3 <sub>0</sub> | 1 |
| 3 | 1 <sub>0</sub> | 2 <sub>1</sub> | 2 <sub>2</sub> | 3 |
| 2 | 0              | 0              | 2              | 2 |
| 2 | 0              | 0              | 0              | 1 |

|      |      |      |
|------|------|------|
| 12.0 | 12.0 | 17.0 |
| 10.0 | 17.0 | 19.0 |
| 9.0  | 6.0  | 14.0 |

|   |   |                |                |                |
|---|---|----------------|----------------|----------------|
| 3 | 3 | 2 <sub>0</sub> | 1 <sub>1</sub> | 0 <sub>2</sub> |
| 0 | 0 | 1 <sub>2</sub> | 3 <sub>2</sub> | 1 <sub>0</sub> |
| 3 | 1 | 2 <sub>0</sub> | 2 <sub>1</sub> | 3 <sub>2</sub> |
| 2 | 0 | 0              | 2              | 2              |
| 2 | 0 | 0              | 0              | 1              |

|      |      |      |
|------|------|------|
| 12.0 | 12.0 | 17.0 |
| 10.0 | 17.0 | 19.0 |
| 9.0  | 6.0  | 14.0 |

|                |                |                |   |   |
|----------------|----------------|----------------|---|---|
| 3              | 3              | 2              | 1 | 0 |
| 0 <sub>0</sub> | 0 <sub>1</sub> | 1 <sub>2</sub> | 3 | 1 |
| 3 <sub>2</sub> | 1 <sub>2</sub> | 2 <sub>0</sub> | 2 | 3 |
| 2 <sub>0</sub> | 0 <sub>1</sub> | 0 <sub>2</sub> | 2 | 2 |
| 2              | 0              | 0              | 0 | 1 |

|      |      |      |
|------|------|------|
| 12.0 | 12.0 | 17.0 |
| 10.0 | 17.0 | 19.0 |
| 9.0  | 6.0  | 14.0 |

|   |                |                |                |   |
|---|----------------|----------------|----------------|---|
| 3 | 3              | 2              | 1              | 0 |
| 0 | 0 <sub>0</sub> | 1 <sub>1</sub> | 3 <sub>2</sub> | 1 |
| 3 | 1 <sub>2</sub> | 2 <sub>2</sub> | 2 <sub>0</sub> | 3 |
| 2 | 0 <sub>0</sub> | 0 <sub>1</sub> | 2 <sub>2</sub> | 2 |
| 2 | 0              | 0              | 0              | 1 |

|      |      |      |
|------|------|------|
| 12.0 | 12.0 | 17.0 |
| 10.0 | 17.0 | 19.0 |
| 9.0  | 6.0  | 14.0 |

|   |   |                |                |                |
|---|---|----------------|----------------|----------------|
| 3 | 3 | 2              | 1              | 0              |
| 0 | 0 | 1 <sub>0</sub> | 3 <sub>1</sub> | 1 <sub>2</sub> |
| 3 | 1 | 2 <sub>2</sub> | 2 <sub>2</sub> | 3 <sub>0</sub> |
| 2 | 0 | 0 <sub>0</sub> | 2 <sub>1</sub> | 2 <sub>2</sub> |
| 2 | 0 | 0              | 0              | 1              |

|      |      |      |
|------|------|------|
| 12.0 | 12.0 | 17.0 |
| 10.0 | 17.0 | 19.0 |
| 9.0  | 6.0  | 14.0 |

|                |                |                |   |   |
|----------------|----------------|----------------|---|---|
| 3              | 3              | 2              | 1 | 0 |
| 0              | 0              | 1              | 3 | 1 |
| 3 <sub>0</sub> | 1 <sub>1</sub> | 2 <sub>2</sub> | 2 | 3 |
| 2 <sub>2</sub> | 0 <sub>2</sub> | 0 <sub>0</sub> | 2 | 2 |
| 2 <sub>0</sub> | 0 <sub>1</sub> | 0 <sub>2</sub> | 0 | 1 |

|      |      |      |
|------|------|------|
| 12.0 | 12.0 | 17.0 |
| 10.0 | 17.0 | 19.0 |
| 9.0  | 6.0  | 14.0 |

|   |                |                |                |   |
|---|----------------|----------------|----------------|---|
| 3 | 3              | 2              | 1              | 0 |
| 0 | 0              | 1              | 3              | 1 |
| 3 | 1 <sub>0</sub> | 2 <sub>1</sub> | 2 <sub>2</sub> | 3 |
| 2 | 0 <sub>2</sub> | 0 <sub>2</sub> | 2 <sub>0</sub> | 2 |
| 2 | 0 <sub>0</sub> | 0 <sub>1</sub> | 0 <sub>2</sub> | 1 |

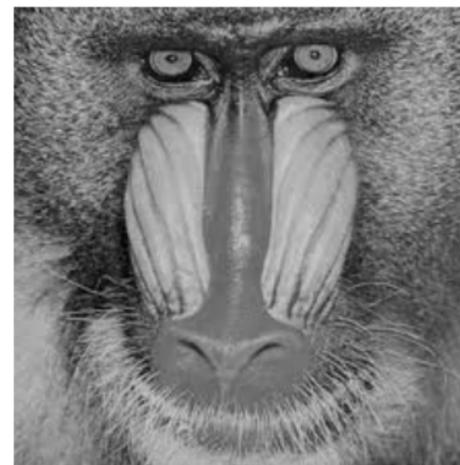
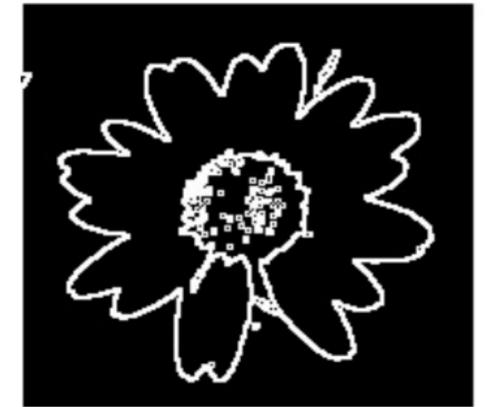
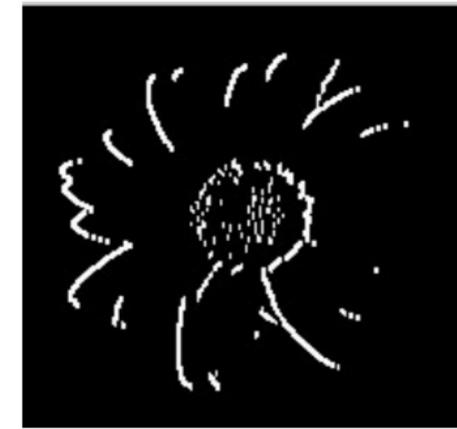
|      |      |      |
|------|------|------|
| 12.0 | 12.0 | 17.0 |
| 10.0 | 17.0 | 19.0 |
| 9.0  | 6.0  | 14.0 |

|   |   |                |                |                |
|---|---|----------------|----------------|----------------|
| 3 | 3 | 2              | 1              | 0              |
| 0 | 0 | 1              | 3              | 1              |
| 3 | 1 | 2 <sub>0</sub> | 2 <sub>1</sub> | 3 <sub>2</sub> |
| 2 | 0 | 0 <sub>2</sub> | 2 <sub>2</sub> | 2 <sub>0</sub> |
| 2 | 0 | 0 <sub>0</sub> | 0 <sub>1</sub> | 1 <sub>2</sub> |

|      |      |      |
|------|------|------|
| 12.0 | 12.0 | 17.0 |
| 10.0 | 17.0 | 19.0 |
| 9.0  | 6.0  | 14.0 |

# Edge Detection

|   |   |    |
|---|---|----|
| 1 | 0 | -1 |
| 1 | 0 | -1 |
| 1 | 0 | -1 |



kernel

|   |   |
|---|---|
| 0 | 1 |
| 2 | 2 |

input

|   |   |   |   |   |
|---|---|---|---|---|
| 1 | 3 | 2 | 1 | 0 |
| 0 | 0 | 1 | 3 | 1 |
| 2 | 1 | 3 | 0 | 3 |
| 1 | 1 | 0 | 3 | 2 |
| 2 | 0 | 1 | 0 | 1 |

output

kernel

|   |   |
|---|---|
| 0 | 1 |
| 2 | 2 |

input

|   |   |   |   |   |
|---|---|---|---|---|
| 1 | 3 | 2 | 1 | 0 |
| 0 | 0 | 1 | 3 | 1 |
| 2 | 1 | 3 | 0 | 3 |
| 1 | 1 | 0 | 3 | 2 |
| 2 | 0 | 1 | 0 | 1 |

output

|  |  |  |  |
|--|--|--|--|
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |

kernel

|   |   |
|---|---|
| 0 | 1 |
| 2 | 2 |

input

|   |   |   |   |   |
|---|---|---|---|---|
| 1 | 3 | 2 | 1 | 0 |
| 0 | 0 | 1 | 3 | 1 |
| 2 | 1 | 3 | 0 | 3 |
| 1 | 1 | 0 | 3 | 2 |
| 2 | 0 | 1 | 0 | 1 |

output

|   |  |  |  |
|---|--|--|--|
| 3 |  |  |  |
|   |  |  |  |
|   |  |  |  |
|   |  |  |  |

kernel

|   |   |
|---|---|
| 0 | 1 |
| 2 | 2 |

input

|   |   |   |   |   |
|---|---|---|---|---|
| 1 | 3 | 2 | 1 | 0 |
| 0 | 0 | 1 | 3 | 1 |
| 2 | 1 | 3 | 0 | 3 |
| 1 | 1 | 0 | 3 | 2 |
| 2 | 0 | 1 | 0 | 1 |

output

|   |   |  |  |
|---|---|--|--|
| 3 | 4 |  |  |
|   |   |  |  |
|   |   |  |  |
|   |   |  |  |

kernel

|   |   |
|---|---|
| 0 | 1 |
| 2 | 2 |

input

|   |   |   |   |   |
|---|---|---|---|---|
| 1 | 3 | 2 | 1 | 0 |
| 0 | 0 | 1 | 3 | 1 |
| 2 | 1 | 3 | 0 | 3 |
| 1 | 1 | 0 | 3 | 2 |
| 2 | 0 | 1 | 0 | 1 |

output

|   |   |   |  |
|---|---|---|--|
| 3 | 4 | 9 |  |
|   |   |   |  |
|   |   |   |  |
|   |   |   |  |

kernel

|   |   |
|---|---|
| 0 | 1 |
| 2 | 2 |

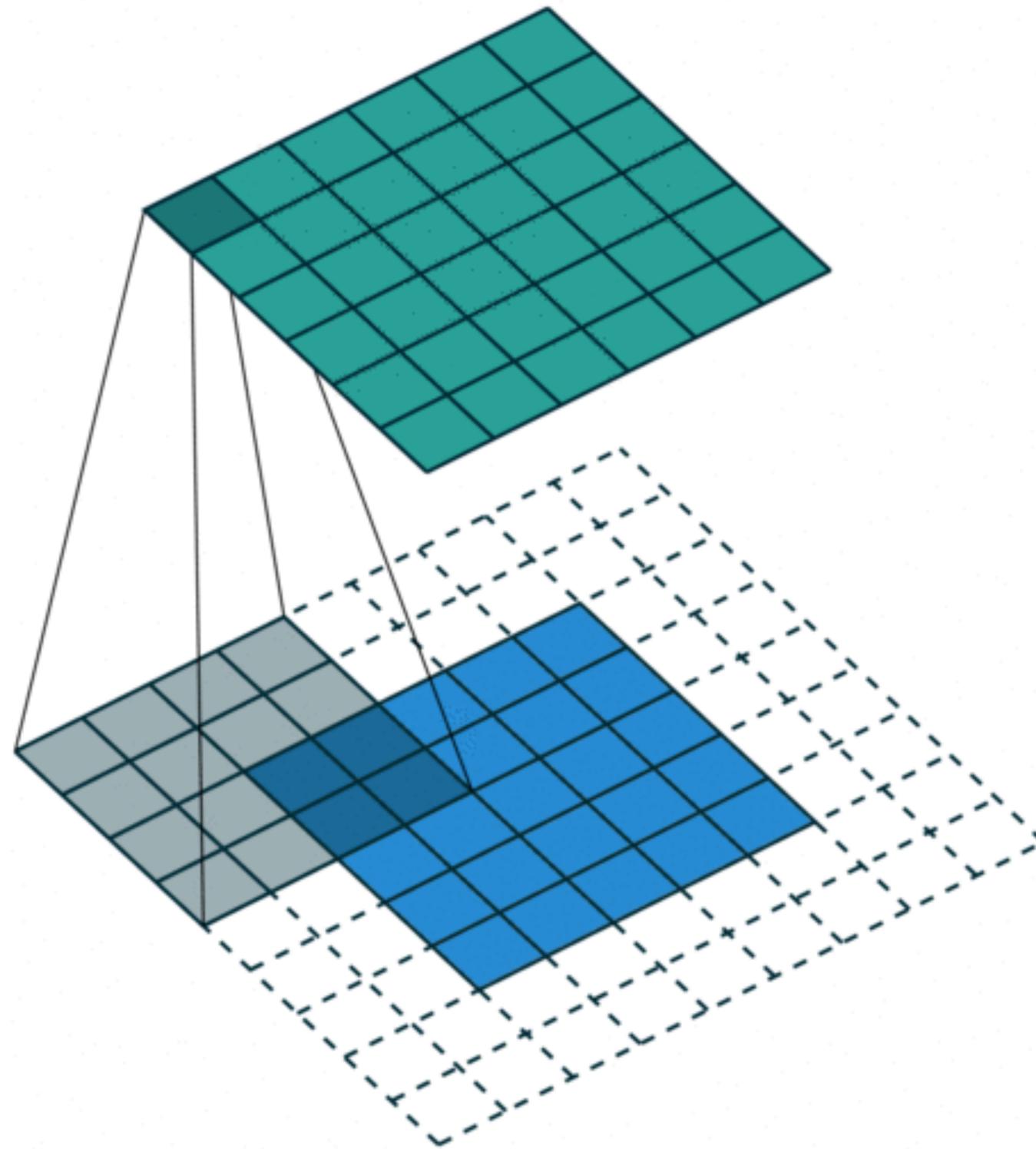
input

|   |   |   |   |   |
|---|---|---|---|---|
| 1 | 3 | 2 | 1 | 0 |
| 0 | 0 | 1 | 3 | 1 |
| 2 | 1 | 3 | 0 | 3 |
| 1 | 1 | 0 | 3 | 2 |
| 2 | 0 | 1 | 0 | 1 |

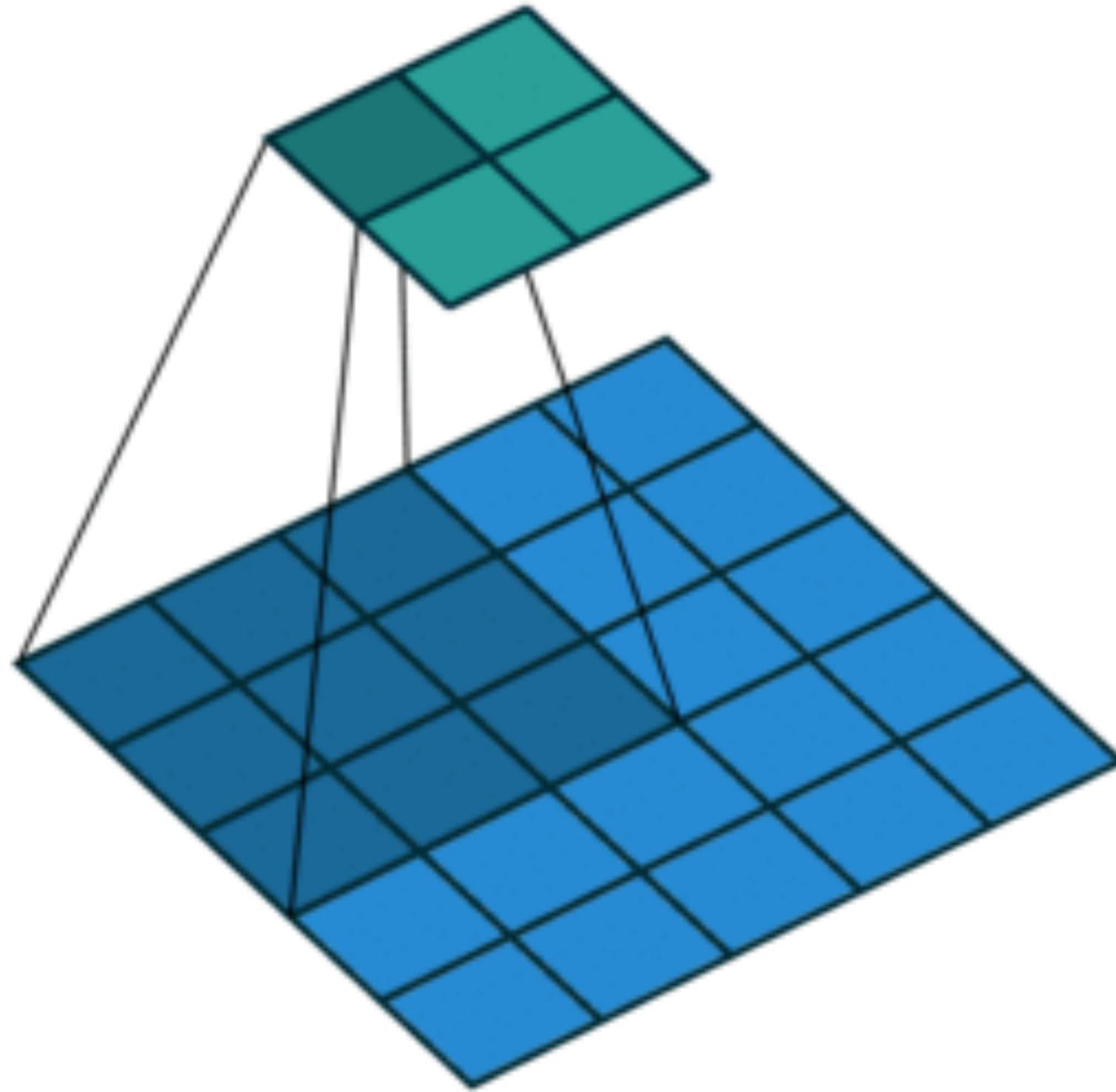
output

|   |   |   |   |
|---|---|---|---|
| 3 | 4 | 9 | 8 |
|   |   |   |   |
|   |   |   |   |
|   |   |   |   |

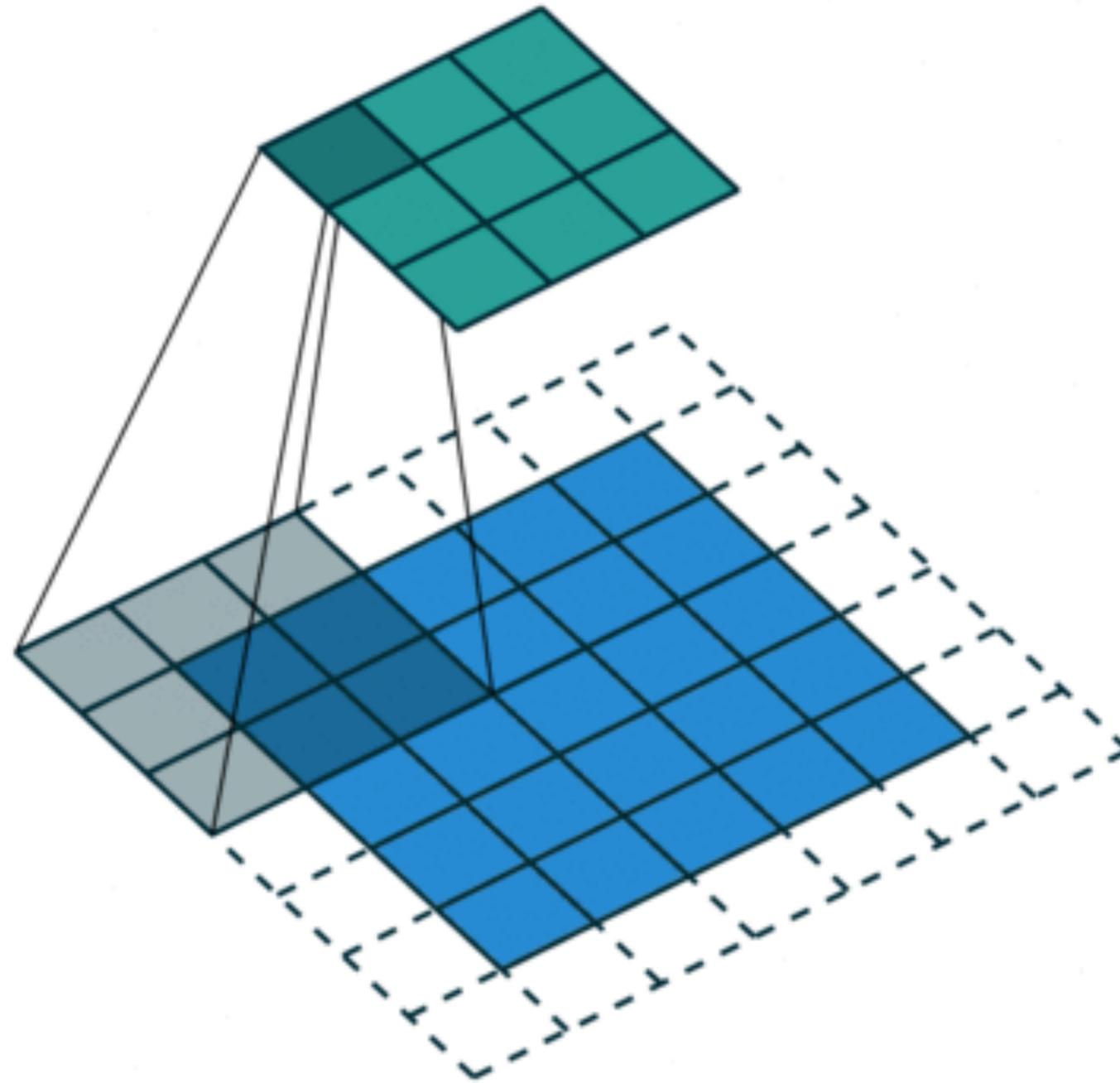
# Padding



# Strides



# Padding and Strides

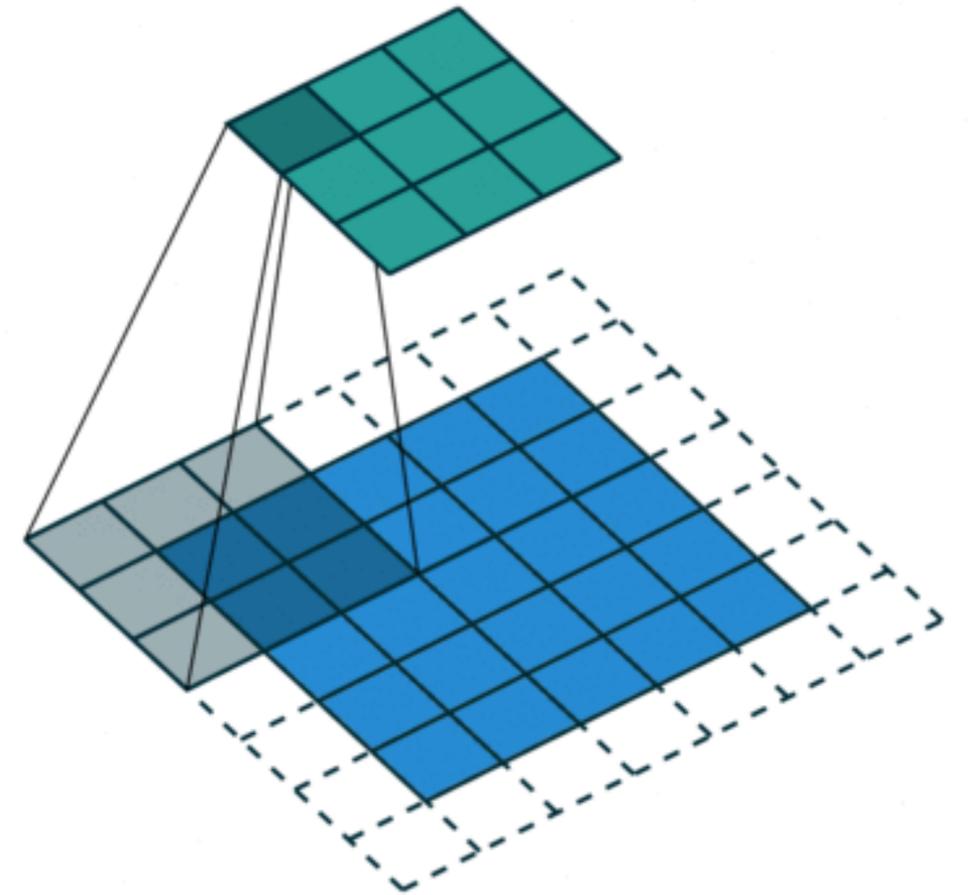


new size

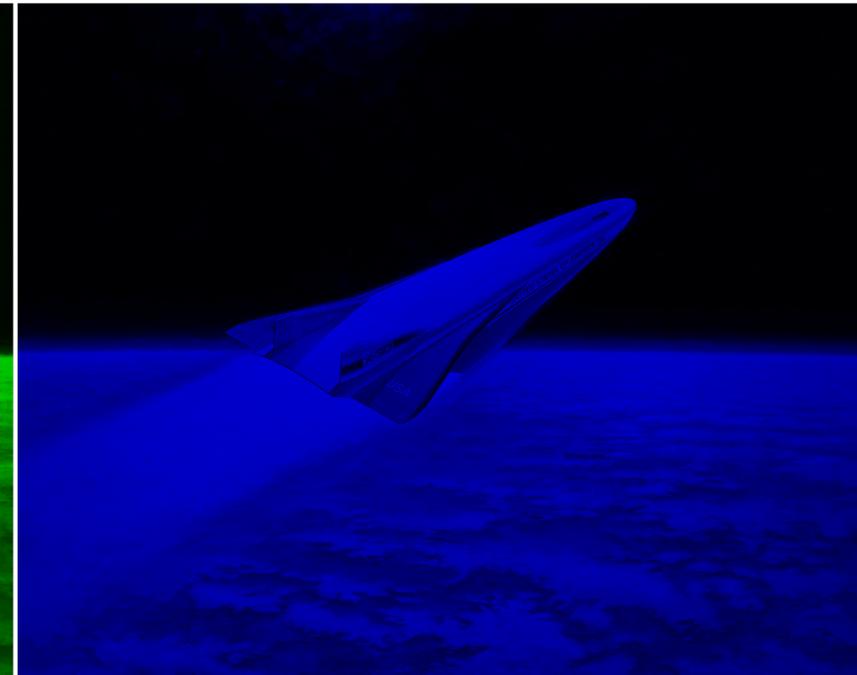
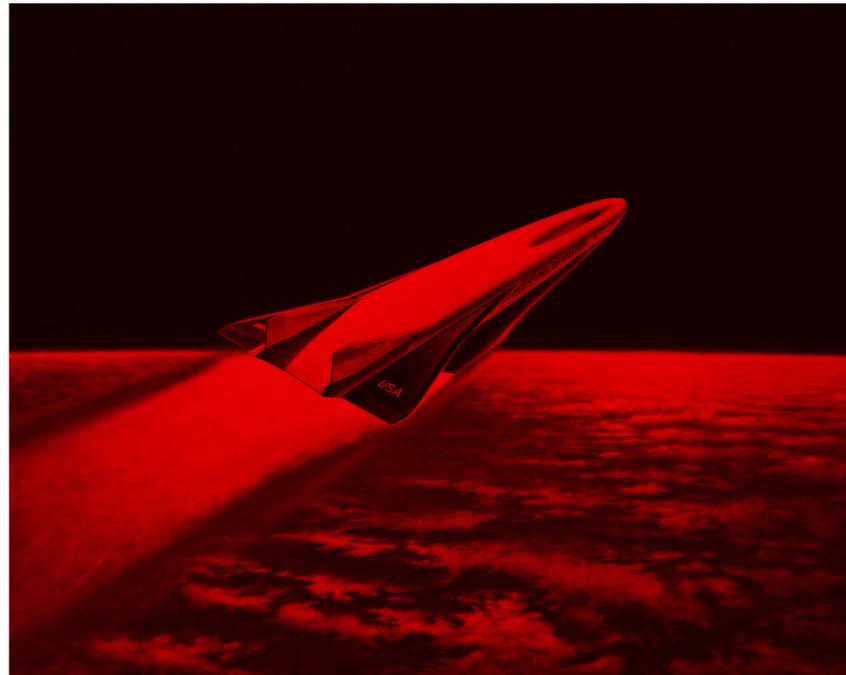
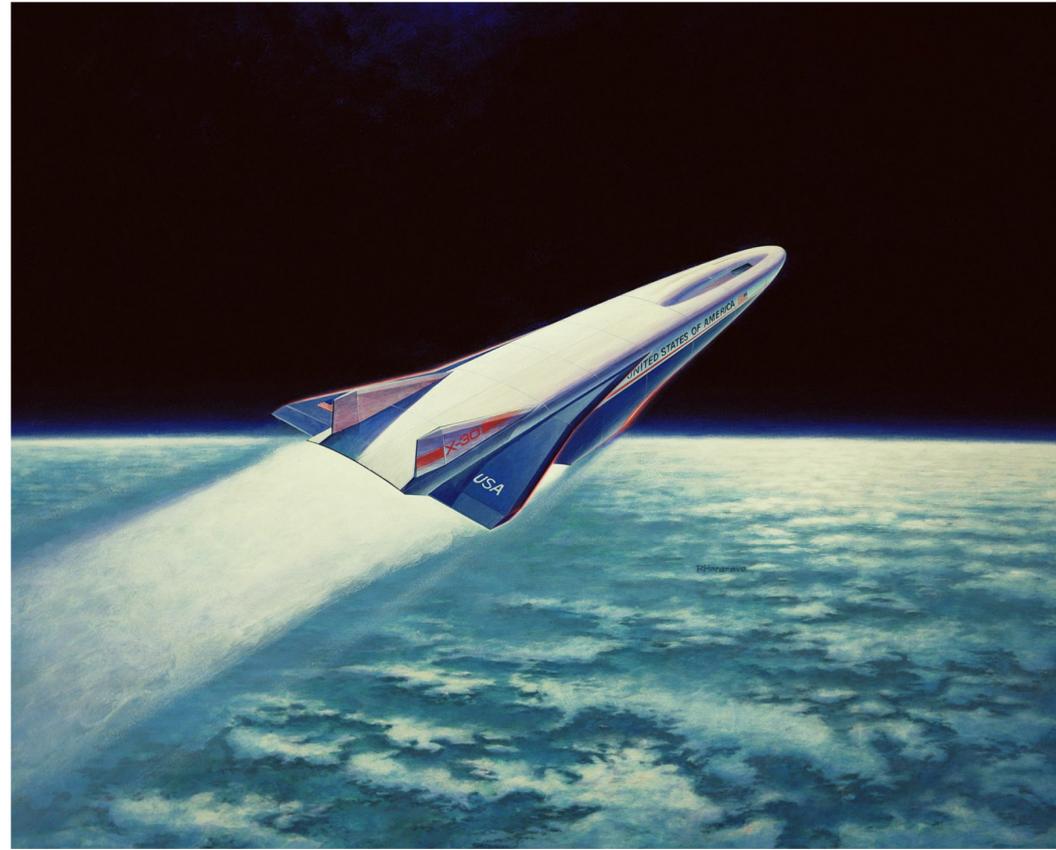
$$H_{out} = \frac{H_{in} - \text{kernel} + (2 \times \text{padding})}{\text{stride}} + 1$$

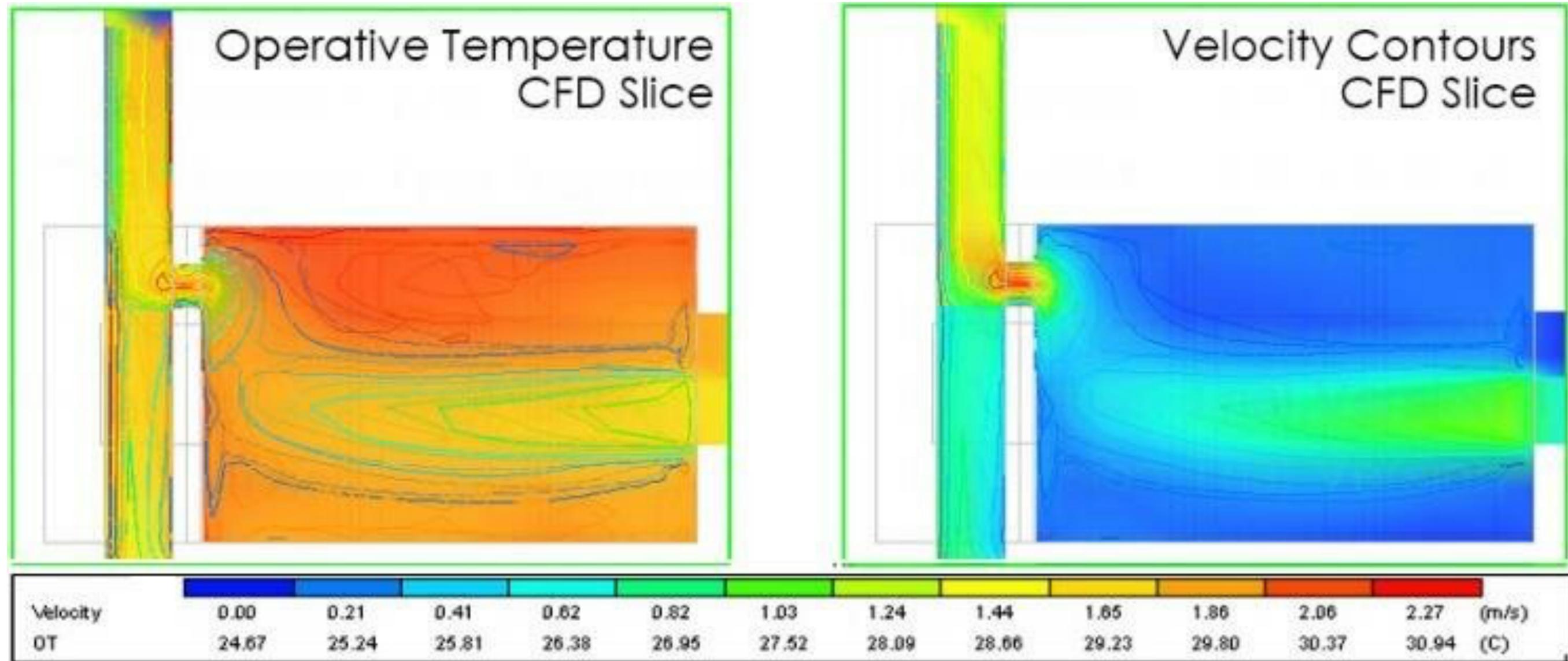
new size

$$H_{out} = \frac{H_{in} - \text{kernel} + (2 \times \text{padding})}{\text{stride}} + 1$$



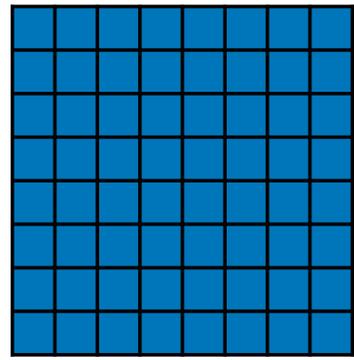
# Channels



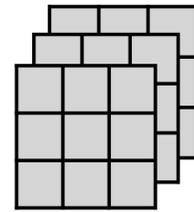


Solar Chimney for Enhanced Natural Ventilation Based on CFD-Simulation for a Housing Prototype in Alexandria, Egypt. Gehad Mekkawi and Rana Elgendy

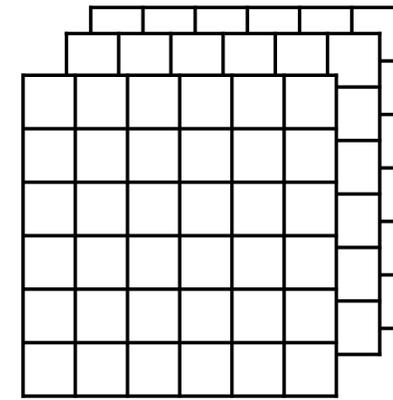
# Multiple Outputs



$$8 \times 8 \times 1$$

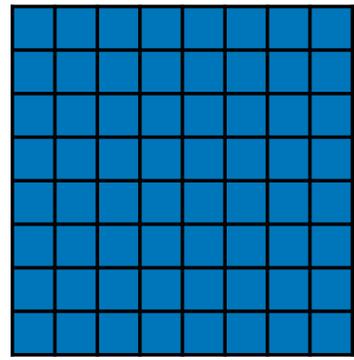


$$3 \times 3 \times 1 \times 3$$



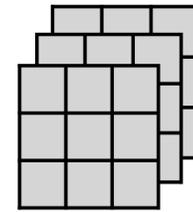
$$6 \times 6 \times 3$$

# Multiple Outputs



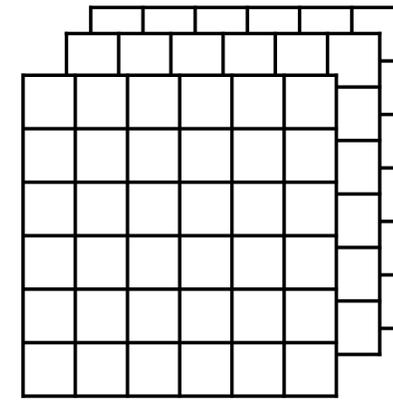
$$8 \times 8 \times 1$$

in channels



$$3 \times 3 \times 1 \times 3$$

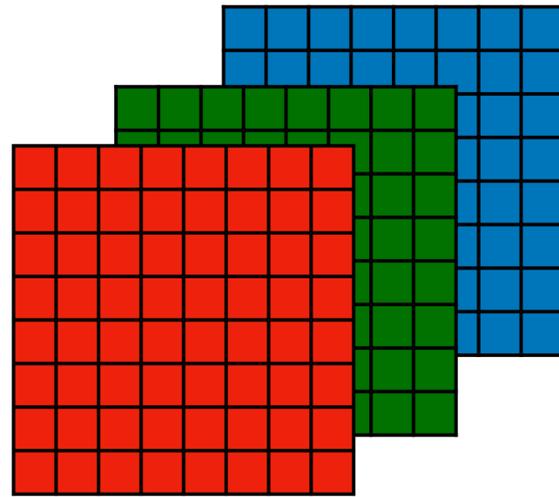
kernel size



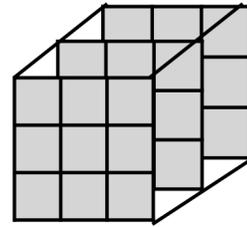
$$6 \times 6 \times 3$$

out channels

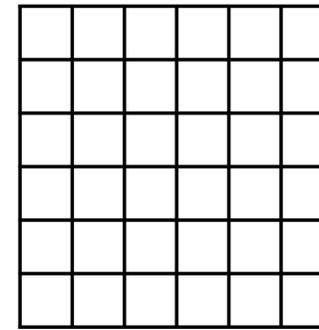
# Multiple Inputs



$$8 \times 8 \times 3$$

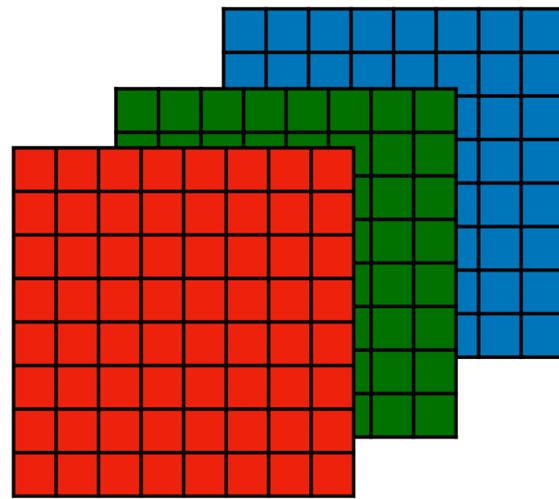


$$3 \times 3 \times 3 \times 1$$



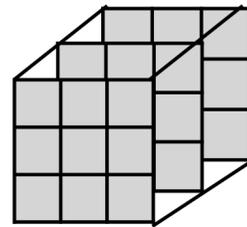
$$6 \times 6 \times 1$$

# Multiple Inputs



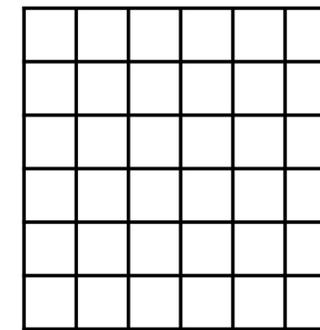
$8 \times 8 \times 3$

in channels



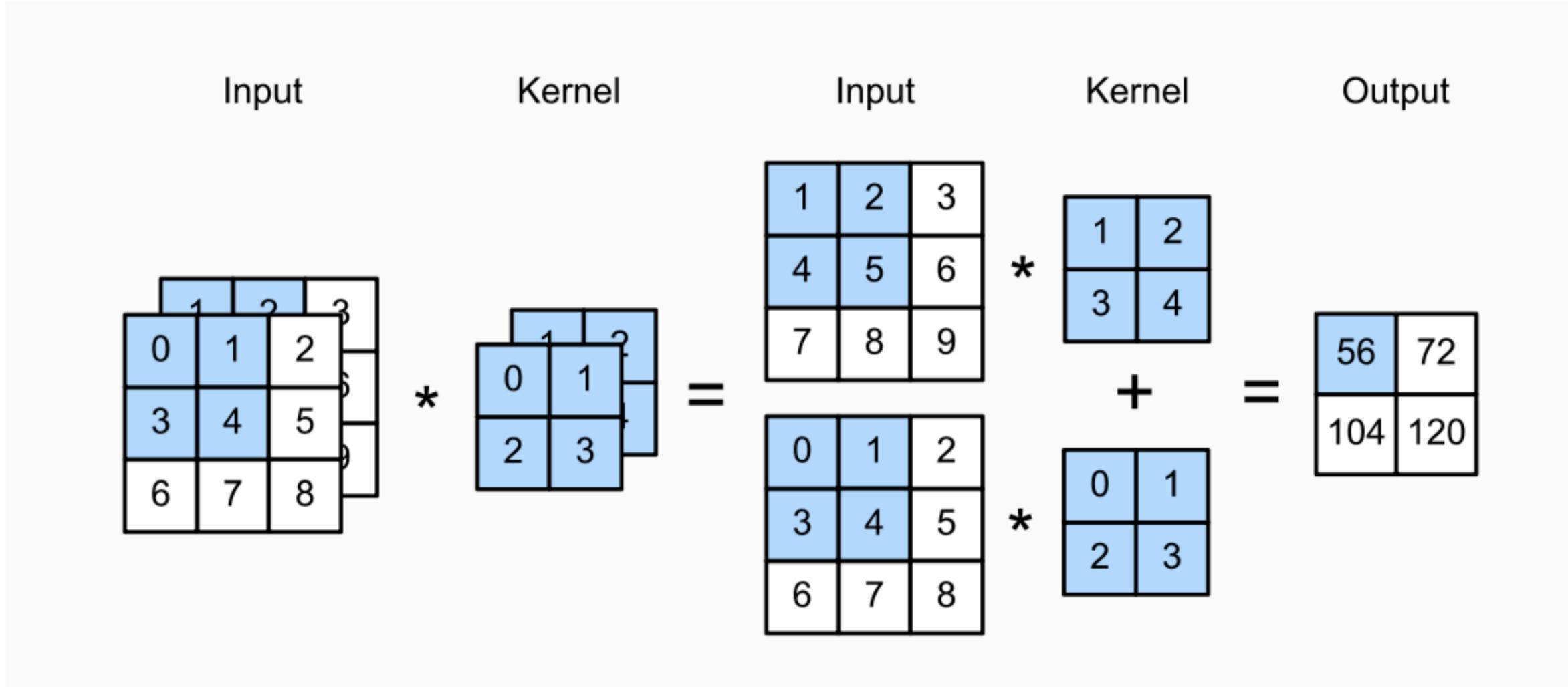
$3 \times 3 \times 3$

kernel size



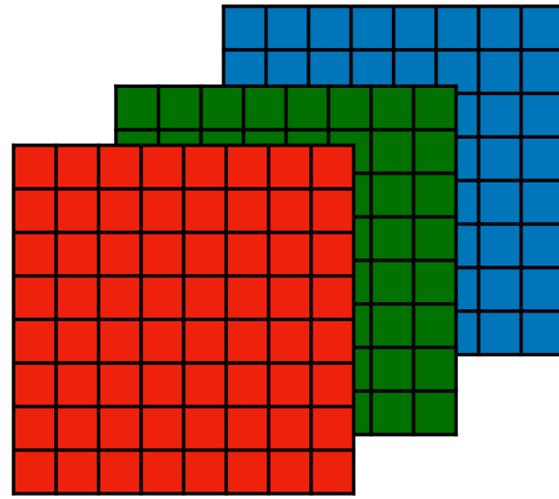
$6 \times 6 \times 1$

out channels

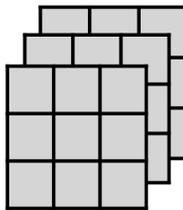
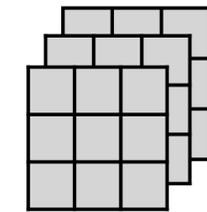


<http://d2l.ai>

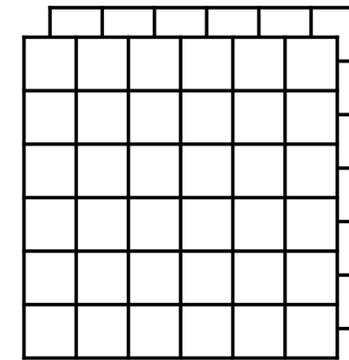
# Multiple Inputs and Multiple Outputs



$$8 \times 8 \times 3$$

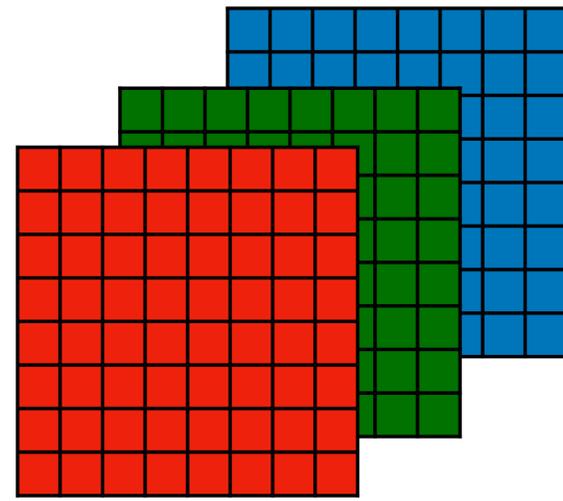


$$3 \times 3 \times 3 \times 2$$



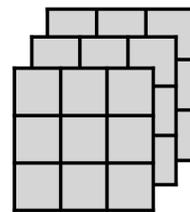
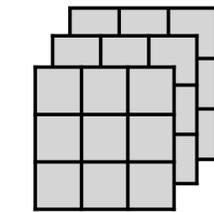
$$6 \times 6 \times 2$$

# Multiple Inputs and Multiple Outputs



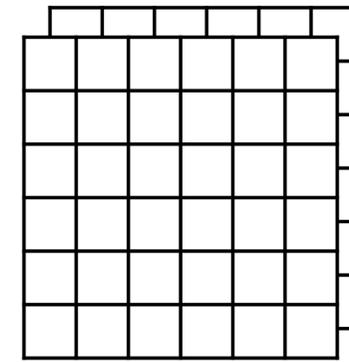
$$8 \times 8 \times 3$$

in channels



$$3 \times 3 \times 3 \times 2$$

kernel size



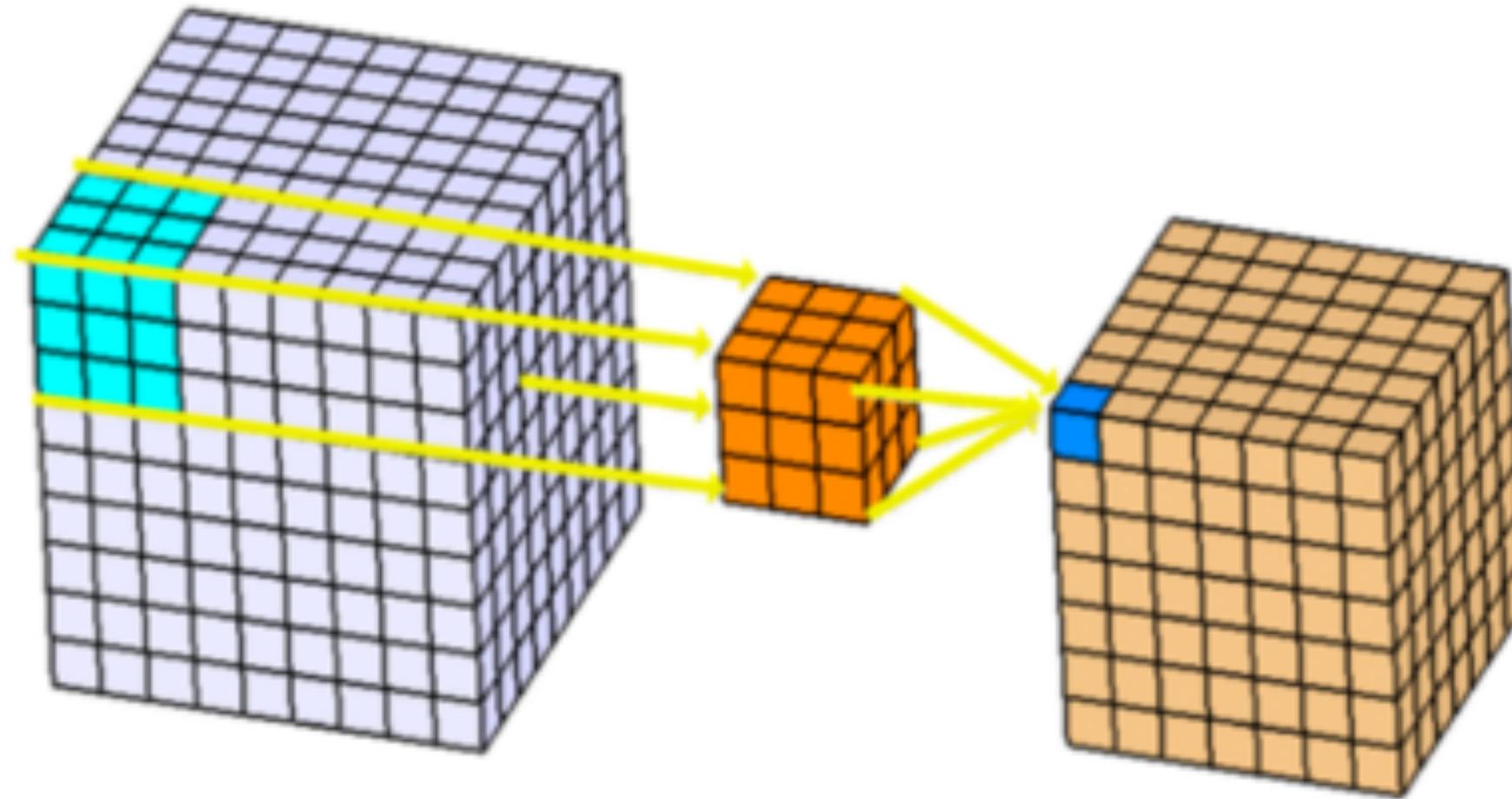
$$6 \times 6 \times 2$$

out channels

# Conv2d

```
torch.nn.Conv2d(in_channels, out_channels, kernel_size, stride=1,  
padding=0)
```

# 3D convolutions



<https://www.kaggle.com/code/shivamb/3d-convolutions-understanding-use-case>

# Pooling

|   |   |   |   |
|---|---|---|---|
| 3 | 2 | 2 | 1 |
| 0 | 3 | 1 | 0 |
| 0 | 1 | 1 | 2 |
| 1 | 1 | 0 | 2 |

max pool

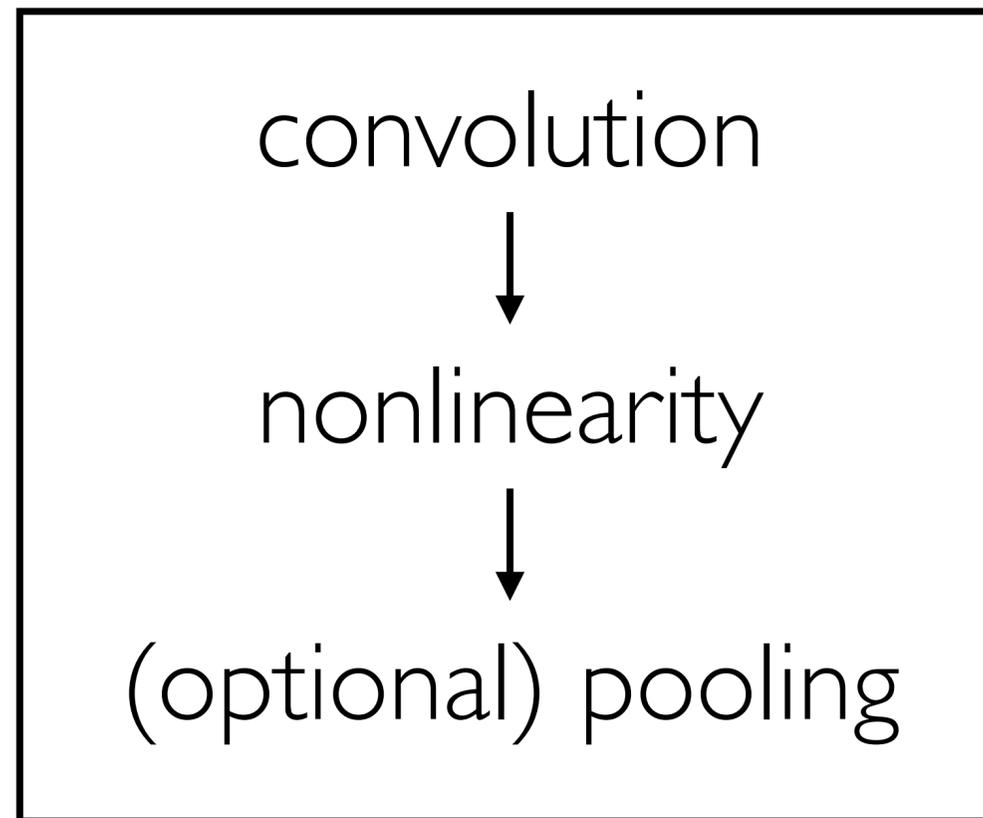
2x2 filter

stride = 2

|   |   |
|---|---|
| 3 | 2 |
| 1 | 2 |

`torch.nn.MaxPool2d`

`torch.nn.AvgPool2d`



(potentially a linear layer(s) after all the convolution layers)