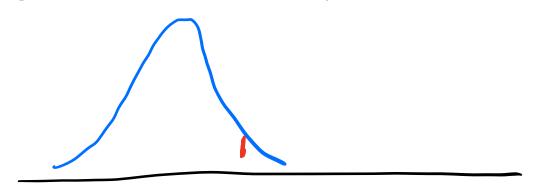
## Hypothesis Tests (two samples)

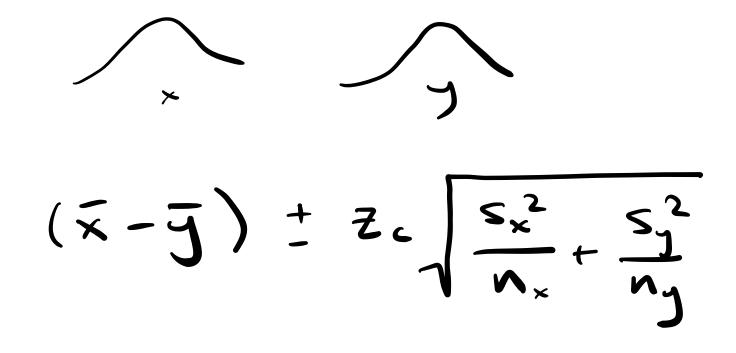
 $\bullet x_k$  $p_k$  $x_2$  $\chi_1$ 

ME EN 275 Andrew Ning aning@byu.edu I introduce a new process that appears to improves yield from 80.5 to 88.6. Is this a significant change or random variation?

My bicycle frame is subjected to a max load of 100.0 and its strength is 110.0. How likely is it to fail?



Recall: confidence interval for difference between two means



Hypothesis test on difference between two means

 $\mu_{x} - \mu_{y} = \Delta$ 

difference is normally distribut) with

mean = D

5.d. =  $\int \frac{S_x^2}{N_x} + \frac{S_y^2}{N_y}$ 

Example

## diameter of inclusions of two types of welds



Is the difference in means significant?

 $f|: M_x - M_y = 0$  $H_a M_x - M_y \neq 0$  $\overline{x} - \overline{y} = -0.03$  $\sigma = \sqrt{\frac{.25^2}{.544} + \frac{.26^2}{.581}} =$ 0.0152 2\*nom. (df (-0.03, 0, 0.0152) = 0.0485

95% confidence bound for difference (argon - co2)?

$$\frac{100000.interval(0.95, -0.03, 0.0152)}{(-0.0598, -0.000000)}$$

Can we conclude that the mean diameter for carbon dioxide welds ( $\mu_y$ ) exceeds that for argon welds ( $\mu_x$ ) by more than 0.015  $\mu$ m?

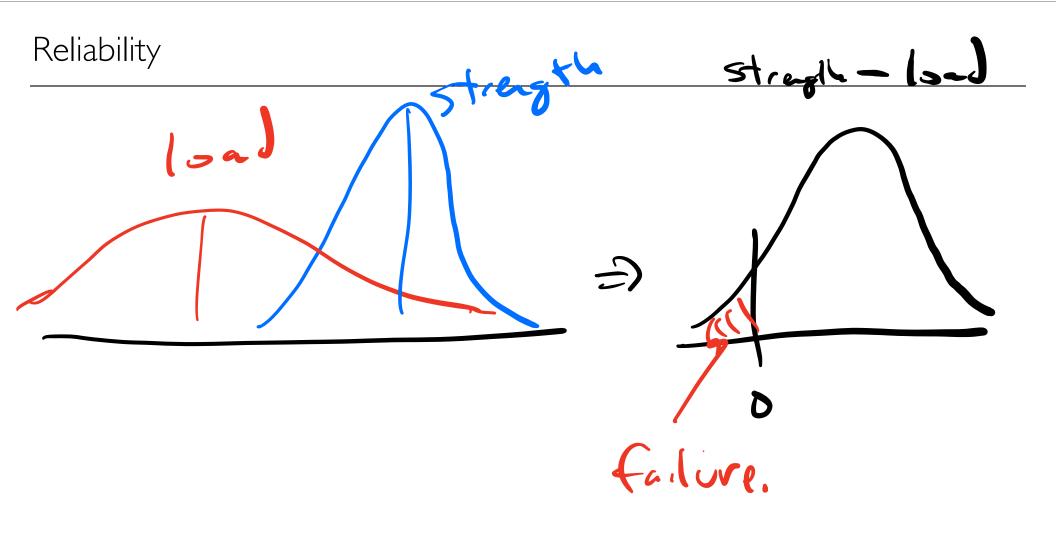
Example

## items identified on website



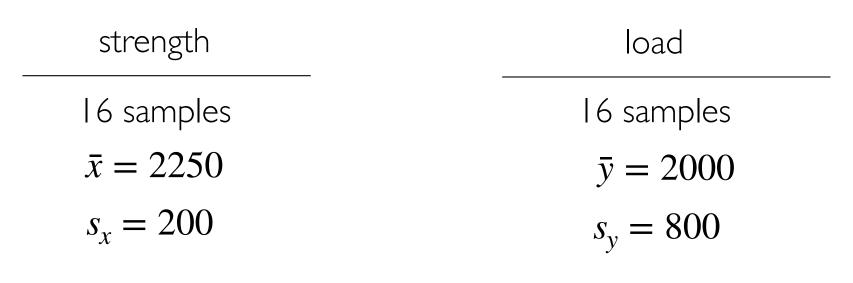
Is the difference in means significant?

95% lower bound on difference



Example

## buckling of bicycle component in axial compression



probability of failure?

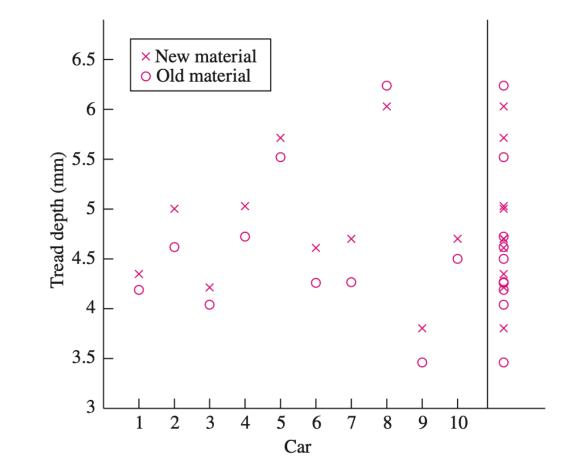
X: strengthe y: load.  

$$M_{x} - M_{y}$$
  
 $\overline{x} - \overline{y} = 250$   
 $T_{x-M_{y}} = \sqrt{\frac{200^{2}}{16} + \frac{800^{2}}{16}} = 206.155$   
Norm.  $cdf(0, 250, 0)$   
 $= 0.112$ 

A tire manufacturer wishes to compare the tread wear of tires made of a new material with that of tires made of a conventional material. One tire of each type is placed on each front wheel of each of 10 front-wheel-drive automobiles. The choice as to which type of tire goes on the right wheel and which goes on the left is made with the flip of a coin.

Statistics for Engineers and Scientists, Navidi

Title Text



<b>TABLE 7.</b> <sup>4</sup>	Depths of tread,	, in mm, for tires	made of new and	old material
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	Car									
	1	2	3	4	5	6	7	8	9	10
New material	4.35	5.00	4.21	5.03	5.71	4.61	4.70	6.03	3.80	4.70
<b>Old material</b>	4.19	4.62	4.04	4.72	5.52	4.26	4.27	6.24	3.46	4.50
Difference	0.16	0.38	0.17	0.31	0.19	0.35	0.43	-0.21	0.34	0.20